How network structure can boost and shape the demand for bus transit

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ABSTRACT

Conventional wisdom states that transit riders are averse to transfers and that consequently bus networks should be designed to limit their number. Probably as a result of this belief, many real bus systems try to connect as many origins and destinations as possible without transfers, so they are usually composed of long, circuitous routes with redundant overlapping sections – and the resulting bus map is hard to understand. If coverage is extensive, many routes are needed. Economics then prevents an agency from populating all routes with sufficient buses to provide attractively frequent service. This low frequency and the complicated circuitous map discourages transfers, perpetuating the belief that people are averse to transferring. Not surprisingly, the percentage of bus trips that includes a transfer has been reported to be: 1.5% for Boston, 3% for New York, 13% for London, and 16% for Melbourne.

The Nova Xarxa in Barcelona was designed with a different paradigm. It was designed and deployed to cover the whole city on the belief that if a bus map is easy to understand, and has direct lines with frequent service and ubiquitous transfer points then the bus system would become more appealing, people would transfer more freely and become users of the network rather than its single lines. With this design paradigm, a city can be covered with fewer lines, which can be depicted on a simple map. The lines can in turn be economically populated with sufficient buses to deliver the high frequency required to encourage transfers. Could this work?

To answer this question and see whether there is truth in the beliefs underlying the new paradigm, this paper examines data from the first three deployment phases of the Nova Xarxa (from 2012 to 2015). It is found that the Nova Xarxa is already attracting more demand than the network it replaced. This attests to its appeal. Furthermore, this demand has increased disproportionately with the number of lines opened for service in each phase, revealing that some people are using the Nova Xarxa as a network. The paper further shows that this growth is underpinned by transfers -- at the end of 2015, the percentage of trips that involved a transfer was approximately 26%, and it reached a maximum of 57% for line V7. These numbers should increase considerably (to 44% and 66%, respectively) once the Nova Xarxa is completed in 2018 and passengers have even more opportunities for transferring. The numbers disprove the conventional wisdom. They strongly suggest that transit providers can attract more demand by providing transfer-friendly networks that can be used as such and not as an inefficient aggregation of individual lines.

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1. Introduction

This paper presents an empirical analysis of a transfer-based bus network, the Nova Xarxa in Barcelona. It attempts to prove two ideas contrary to conventional wisdom: (a) that transit passengers are much less averse to transfers than assumed in current planning practice, and (b) that properly designed transfer-based networks can be very appealing and even attract more demand than their conventional counterparts. To do so, the analysis examines the jumps in demand as new lines and connections were opened in the transfer-friendly Nova Xarxa. The observed patterns are found to exhibit a strong network effect, which cannot be explained without a high percentage of transfers. It is also found that the new system attracts considerably more demand than the network it is replacing, attesting to its appeal.

Two bus network design concepts are generally considered by transportation planners: direct-service and transfer-based (Vuchic, 2005; Dodson et al., 2011). The main difference between the two is how origin and destination pairs are connected. The former encourages direct trips, so most users can complete their travel using a single line. The latter also connects some origin-destination pairs directly, but most are not, so transfers are considered an integral part of the design.

Conventional wisdom dictates that transfers should be minimized since users perceive them negatively. The idea is supported by different studies summarized in Currie (2005), which quantify the time penalty equivalent to a bus-to-bus transfer to be between 5 and 50 min for the connections in the systems studied. Therefore, many planning efforts have focused on direct-service strategies. In this spirit, some network design models strive to minimize the number of transfers (e.g., Zhao, 2006), while others constrain their number (e.g., Baaj and Mahmassani, 1995).

In some cases, however, transfer-based networks might be better able to satisfy dispersed mobility patterns. This idea is supported by analytical studies (Thompson, 1977; Daganzo, 1987; Badia et al., 2016) and, to some extent, by empirical studies that have compared different regions with different network types (Schimek, 1997; Thompson and Matoff, 2003; Brown and Thompson, 2008, 2012). These empirical studies are somewhat limited, however, because they lack longitudinal data. And unlike the work to be presented, they do not focus on the stimulation of demand, transfers or the network effect.

To maximize their appeal, transfer-based networks should have three properties: (i) provide full area coverage with easy transfers and non-circuitous routings; (ii) be easy to understand (e.g. a pure grid); and (iii) operate with high frequency. These features should reduce riders’ aversion to transfers and encourage usage; see Mees (2000) and Nielsen et al. (2005).

The Nova Xarxa is unique in that it is the first instance in which a complete direct-service network is being replaced by a transfer-based network that meets the three conditions above. The design is based on plans outlined in Estrada et al. (2011) and the model in Daganzo (2010). The Nova Xarxa’s rollout started in 2012, and after several intermediate deployment phases should be completed in 2018. This gradual deployment has created an excellent natural experiment to test the validity of ideas (a) and (b) above with the longitudinal data that it has generated.

The paper describes these tests. It is organized as follows. Section 2 provides background; it compares Barcelona’s pre-existing network with the Nova Xarxa. Section 3 describes the evolution of bus boardings in the Nova Xarxa from 2012 to 2015, which unveils a significant network effect. Then, Section 4 presents the results of a demand analysis that estimates transfers and establishes the validity of ideas (a) and (b). Finally, Section 5 presents some conclusions.

2. Barcelona’s bus system: the network redesign

Barcelona’s old urban bus network had 63 direct-service lines with many centripetal routes. The new bus network, the Nova Xarxa, will serve the whole city with 28 lines and replace most of the old bus network so that only 20 secondary routes of the old network will be retained. The Nova Xarxa will be formed by 8 horizontal lines, 17 vertical and 3 diagonal. The latter will serve three major corridors and be superimposed on a rectangular grid formed by the rest. As of 2015, thirteen of these lines have been opened to the public. Fig. 1 shows the 2015 network side by side with the old system. These two maps show that from a user’s perspective, both networks display property (i) above. However, only the Nova Xarxa exhibits property (ii), unlike the old system. The new network has and will continue to have full coverage with non-circuitous routes that are clearly shown on the map.

Property (ii), understandability, is further reinforced by navigational aids on the street and in the buses. Fig. 2 shows the diagrams that are provided at transfer locations. These diagrams include: the lines that serve the transfer point, their directions, the station locations, and the recommended walking paths for connecting passengers.

Now consider property (iii), high frequency. The Nova Xarxa will eventually be served by 573 buses with an average headway of 6.18 min, similar across all lines. Contrast this with the old bus network which was served by 761 buses with an average headway of 12.30 min. Thus, the Nova Xarxa will use fewer buses but deliver nearly twice the service frequency of the old network. Stop spacings have also changed in the Nova Xarxa. They were increased, but mostly in the periphery because most of the stops in the city center remained where they were, and any relocations were slight. As a result of this policy the city-wide average stop spacing increased to 367 m, as compared to 330 m for the lines that were removed.

The new network is also friendlier towards transfers than the old for three different reasons. First, the increased frequency reduces transfer times. Second, the average distance walked for transfers has been reduced thanks to strategic bus stop relocations. And third, transfers have become easier to understand thanks to the network’s simpler structure, the more intuitive location of transfer stops and the increased presence of navigation aids.

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1 The walking distance reduction varies across transfer points. In cases where stops were relocated, the transfer walking distance was reduced up to three times. That is the case of the transfer between lines H6 and V21, as compared with old lines L74 and L10.
Fig. 1. Maps of the old bus network and the Nova Xarxa in 2015. Source: http://www.tmb.cat/.
Finally, it is also important to note that the fare structure is not a distinguishing factor between the pre-existing network and the new design. Fares in Barcelona were, and continue to be completely flat across all transit modes; and transfers are free if made within 1 h and 15 min from the start of a trip. This fare integration, which favors transfers, has been in place since 2000—well before the *Nova Xarxa* was begun and for the whole duration of our study.

### 2.1. Gradual implementation process until 2015

Barcelona’s old bus network was in full operation until September 2012, when the first instalment of the *Nova Xarxa* was opened to the public. At that time redundant lines of the old network were eliminated. By December 2015, two more portions of the *Nova Xarxa* had been opened, and two more sets of old redundant lines had been eliminated. Table 1 summarizes the characteristics of the new lines, and lists the old lines they replaced.

As Table 1 shows, the new lines are being operated with slightly longer headways than those planned for the final phase. This occurs because the agency has to devote bus resources to populate many old lines that cannot be removed because they serve O-D pairs not yet covered by the new network. Since there will be few of these O-D’s in the final phase, the idea is to increase the frequency of the new routes to their final targets at that time, when few old lines will have to be retained and populated. As of December 2015, 235 vehicles served the 13 new lines implemented to date.

### 3. Raw data interpretation: the number of bus boardings and the network effect

To see how the network configuration influences travel we tracked the number of ticket validations per month for every line as the network was expanded. In both the old and the new systems, users validate their tickets upon boarding every bus, including transfers. Therefore, validations slightly overstate the number of trips taken by paying customers, since some trips involve more than one boarding. Data collection started in October 2012 when the first lines were opened to the public, and ended in October 2015.

The solid line of Fig. 3(a) shows that the total number of validations in the *Nova Xarxa* consistently increased when new lines were opened. This is not surprising since the service was being expanded. A bit more surprising, however, is the fact that if we group the lines by the phase in which they were implemented (see the dotted and dashed lines labelled “Phase 1”, “Phase 2” or “Phase 3”) one can see how after each transition, the validations on each set of lines increased to a new baseline level. The actual changes can be more clearly seen in Fig. 3(b) and (c), which superimpose the yearly profiles of these validations.

The observed jumps in validations from one phase to the next strongly suggest that the implementation of new bus lines leads to an increase in the boardings of pre-existing lines, most likely due to the new connections and the possibility to link

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2 The 4th year is incomplete. It belongs to Phase 3 and consists of a single month (October) which is marked in the figures by a thick dot. As one might expect, the dot coincides in both cases with the corresponding point for the previous October, which is also in Phase 3.
more origin-destination pairs with a single transfer. In other words, the jumps likely are a manifestation of the network effect that arises when high-frequency lines provide extended coverage to an entire region.

The evidence is fairly conclusive. The jumps in the curves of Fig. 3 are unlikely due to seasonal effects since the curves show similar profiles in different years and their jumps are quite pronounced. In particular, note that the number of boardings for the lines of Phase 1 grew by about 31.7% as Phases 2 and 3 were completed. Furthermore, this notable growth in boardings for specific lines cannot be attributed to an improving economy or any other factor that could stimulate the demand for transportation. During the study period, Barcelona’s overall transit ridership (including Metro, light rail and all bus services) and private vehicle demand levels remained approximately unchanged. This is shown by the solid line of Fig. 4, which tracks the number of overall transit trips from 2011 until 2014. The line decreases by 2.1% in a very narrow band. The pattern is almost identical for private vehicle trips. This is shown by the dashed line, which decreases by 3.2% between 2011 and 2014. These declining numbers indicate that the boarding increases seen in the Nova Xarxa were not the result of a benign economic climate or an overall increase in the city’s demand for mobility.

Further supporting the presence of network effects is that positive jumps in boardings were consistently observed for all lines and all phases. In particular, as shown by the dotted line marked with triangles in Fig. 4, the aggregate boardings on Phase 1 lines increased 20.3% from Phase 1 to Phase 2 and by another 9.5% from Phase 2 to Phase 3. The growth in boardings by the lines deployed in Phase 2 is best captured by ignoring line H16 because this line was not held fixed. Line H16 was extended so substantially in Phase 3 that its validations quadrupled. The fixed lines that remained grew by 24.2% from Phase 2 to Phase 3, as depicted by the dotted line marked with circles in Fig. 4.

In summary, this section has established that the Nova Xarxa’s lines exhibit: (i) boarding volumes that have increased at a higher pace than any of their transit or private vehicle alternatives; and (ii) jumps in these boardings that occur as new lines are deployed. All of the above points to the appeal of the new system and the existence of a positive network effect that arises with the implementation of new lines. Passengers must be taking considerable advantage of transferring opportunities. The next section estimates the number of passenger trips taken (the demand) for each line, and the percent that transfer.

### 4. Analysis: Trips taken and the percent that require transfers

Because only ticket validations are observed a model was constructed to break these validations into transfers and initial boardings. Since the latter correspond to trips taken, this breakdown enabled us to assess the growth in travel demand, and in the percent of demand that requires transfers. This section focuses on the results of this model, and only describes its logic qualitatively. A full description is given in Appendix A.

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**Table 1**

<table>
<thead>
<tr>
<th>Phase (Date open)</th>
<th>Line</th>
<th>Current headway (min)</th>
<th>Design headway (min)</th>
<th>Bidirectional Length (km)</th>
<th>Old bus line (removed)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 (10/1/12)</td>
<td>H6</td>
<td>6.0</td>
<td>5.0</td>
<td>9.7</td>
<td>L74</td>
</tr>
<tr>
<td></td>
<td>H12</td>
<td>6.0</td>
<td>3.0</td>
<td>11.4</td>
<td>L56</td>
</tr>
<tr>
<td></td>
<td>D20</td>
<td>6.0</td>
<td>4.0</td>
<td>9.2</td>
<td>L57, L157</td>
</tr>
<tr>
<td></td>
<td>V7</td>
<td>7.0</td>
<td>7.0</td>
<td>5.1</td>
<td>L30</td>
</tr>
<tr>
<td></td>
<td>V21+</td>
<td>7.0</td>
<td>6.0</td>
<td>8.2 (9.5)</td>
<td>L10</td>
</tr>
<tr>
<td><strong>Total</strong></td>
<td></td>
<td></td>
<td></td>
<td><strong>84.1</strong></td>
<td></td>
</tr>
<tr>
<td>2 (11/18/13)</td>
<td>H8</td>
<td>6.5</td>
<td>5.0</td>
<td>13.0</td>
<td>L15</td>
</tr>
<tr>
<td></td>
<td>H10</td>
<td>6.5</td>
<td>3.0</td>
<td>13.2</td>
<td>L43, L44</td>
</tr>
<tr>
<td></td>
<td>H16b</td>
<td>7.5</td>
<td>5.0</td>
<td>Ph. 2: 4.0 – Ph. 3: 12.2</td>
<td>Ph. 2: L14', L36', L41' – Ph. 3: L9</td>
</tr>
<tr>
<td></td>
<td>V3+</td>
<td>7.0</td>
<td>5.0</td>
<td>7.5 (8.7)</td>
<td>L72</td>
</tr>
<tr>
<td></td>
<td>V17</td>
<td>7.0</td>
<td>6.0</td>
<td>8.8</td>
<td>L28, L19', L40</td>
</tr>
<tr>
<td></td>
<td>Partial</td>
<td></td>
<td></td>
<td></td>
<td><strong>182.2</strong></td>
</tr>
<tr>
<td><strong>Total</strong></td>
<td></td>
<td></td>
<td></td>
<td><strong>243.5</strong></td>
<td></td>
</tr>
<tr>
<td>3 (9/15/14)</td>
<td>H14</td>
<td>8.0</td>
<td>8.0</td>
<td>8.1</td>
<td>L141</td>
</tr>
<tr>
<td></td>
<td>V15</td>
<td>6.5</td>
<td>4.0</td>
<td>8.7</td>
<td>L17, L16</td>
</tr>
<tr>
<td></td>
<td>V27</td>
<td>8.0</td>
<td>8.0</td>
<td>11.1</td>
<td>L71</td>
</tr>
<tr>
<td></td>
<td>Partial</td>
<td></td>
<td></td>
<td></td>
<td><strong>61.3</strong></td>
</tr>
<tr>
<td><strong>Total</strong></td>
<td></td>
<td></td>
<td></td>
<td><strong>243.5</strong></td>
<td></td>
</tr>
</tbody>
</table>

* These lines cross a tunnel where there are no stops. For this reason, the tunnel length is removed. The total bus line length is displayed in parenthesis.

* This line was implemented in Phase 2 but was extended in Phase 3, for this reason, two lengths are displayed.

* These lines were shortened to avoid overlap with the new lines, but not totally removed.

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\[3\] The only months that do not exactly conform to this pattern are the first months after the implementation of new lines (October 2012 for Phase 1, November 2013 for Phase 2 and September 2014 for Phase 3). In all cases, the validations for these initial months were lower than in the following years. One of the reasons for this is that the new lines did not start their operation until the middle of the month.
If transit users were to avoid transfers, one would expect demand levels in already deployed lines not to be affected as new lines are implemented. Therefore, it stands to reason that the demand and the percentage of transfers can be teased out from the longitudinally observed growth in validations per line by examining its statistical relationship to the fixed length of the line and the growing length of the connecting lines. As explained in the appendix, a parsimonious two-parameter regression model does the job. The model predicts both the number of monthly passenger trips and the number of monthly passenger trips with a transfer, for each line during each of the network deployment phases.

The model’s two parameters are assumed to be different for each line. Therefore, they were separately estimated across them. Only lines opened in Phase 1 were considered because only they contained sufficient longitudinal information to estimate their parameters. Opened in Phase 1, line D20 was excluded because its parameters could not be reliably estimated. This left lines H6, H12, V7 and V21. For maximum statistical efficiency, all data from Phases 1–3 were used. Only lines opened in Phase 1 were selected because (i) they were longitudinally observed the longest (under three different network configurations); and (ii) their basic demand (without transfers) was easier to isolate without specification error because Phase 1 included the fewest connecting lines. The resulting model was then applied to all the lines and phases, past and future, to predict the demand and the percent that involves transfers.

Table 2 displays the predictions. For each line and implementation phase, the table includes the total monthly demand, the number of transfers, and the corresponding percentage. The values obtained indicate that the number of validations

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4 D20 is a diagonal line in the periphery that is connected at sharp angles to other lines. As a result, many of its connecting paths are too circuitous to be practical. This feature makes estimation less reliable because it requires assumptions about route choice.
involving transfers increases with successive phases to a considerable fraction of the total. In the third phase, 26% of the trips involve a transfer, and for line V7 the number rises to 57%. These values are expected to increase further as new Nova Xarxa lines are deployed in the phases to come. Ultimately, the model predicts that transfers will represent more than 44% of all trips in the final phase and almost 66% for line V7. Thus, it seems apparent that given the right conditions and contrary to conventional wisdom passengers will embrace transfers. In other words, the results strongly support idea (a) of the introduction.

It is also worth noting that transfers seem to be occurring because the network was designed to encourage them. The Nova Xarxa’s current 26.4% value already exceeds by a wide margin the transfer percentages of the old bus network, which was about 11% (Transports de Barcelona, 2016). Both the current and forecasted values are also much higher than the percentage of transfers in other urban bus networks that are less transfer friendly: Melbourne 16% (Currie and Loader, 2010), or Boston 1.5%, London 13% and New York 3% (Guo, 2008). These numbers are consistent with the idea that a network designed for transfers can attract transfers. They also suggest that such a network could also attract more demand than a direct-service network – idea (b) of the introduction.

Further analysis confirms this idea. That new demand is stimulated by the new network can be seen by comparing the demand of the new lines versus those that they replaced. To compare apples with apples we verified from the map that the replaced lines had similar or better coverage than the new lines. This is weakly confirmed by the rough similarity in the monthly demands of the new and replaced lines, which are shown on the first two rows of Table 3.\(^5\) So, to test idea

\(^5\) For the new lines, the table displays the estimated monthly trips with zero transfers; i.e., the difference between the 7th and 8th lines of Table 2. The values for line V7 are dissimilar because V7 is considerably shorter than the line it replaced.
(b), compare now row 1 with row 3, which displays the current total monthly demand of the new lines in Phase 3. This approximates the extra demand due to the improved connectivity, ease of use and level of service of the transfer-based network. As can be seen from the table, the difference exceeds 20% for lines H6, H12 and V7, and is about 6% for line V21. This strongly supports idea (b) – that a properly designed transfer-based network can induce extra demand.

5. Conclusions

Analysis of the Nova Xarxa shows that a well-designed transfer-based network can attract new users, and that these users will not be averse to transferring. The acceptance of transfers by transit users not only means that more trips can be completed using a network but that an agency can operate more effectively by consolidating service in well-connected, high-frequency corridors.

In the case of Barcelona, the case study reveals that the new lines are already serving more demand than the pre-existing lines they replaced. Furthermore, the current levels have been reached after a gradual increase concurrent with the expansion of the network. This increase contrasts with a slight declining trend for all transportation modes. This strongly suggests that the growth in demand is due to network effects of the new design and not to other economic, social, or urban factors.

The results also show that the new network is drastically reshaping the demand. While conventional bus networks in big cities exhibit transfer percentages ranging from 1.5% to 16%, the Nova Xarxa current percentage is 26% -- and this value is projected to rise to 44% when the number of lines is expanded from 13 to 28 at the project’s completion in 2018. These considerable numbers support the notion that transit users will transfer if given an attractive chance.

In view of these findings we recommend that transfers be systematically considered as an integral part of bus network design, much as when considering subway systems. The case study in this paper shows that, properly designed, transfer-based bus networks can capture much demand and be an effective mobility solution for many cities.

Acknowledgments

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Appendix A. Technical analysis

A.1. Demand model

A parsimonious regression model is proposed. It assumes that the total number of validations in a line, \( V_k \), arises from two demand types: (i) direct trips, where origin-destination pairs can be served without a transfer and therefore must lie in the influence area of line \( k \); and (ii) one-transfer trips for origin-destination pairs requiring transfers.\(^6\) To simplify the analysis, we assume that the generation rates for trips of type (i) and (ii) are uniform in space for each line, although they can vary across lines. Except where indicated, the model shall assume that the influence areas of the various lines, where trips are generated, do not overlap.

Although a detailed analysis would take into consideration the station-to-station O-D demands and a route assignment, this can be avoided here because Barcelona’s network closely resembles a homogeneous rectangular grid. To see how this helps, assume for the moment that the grid is perfect with no overlaps and similar frequencies everywhere where people choose the shortest path. Furthermore, since the stop spacing is practically constant, ignore the stops and assume that people walk to/from the closest line. Also let’s (reasonably) assume that each line has a catchment area of uniform width where the trip generation rates for direct trips and 1-transfer trips are uniform. These rates are assumed to be proportional to the

\(^6\) We verified with a regression analysis not included in this appendix that the number of passengers making more than one transfer is negligible. Therefore O-D pairs requiring more than one transfer are not considered in the model.
number of destinations in the respective catchment areas. It is then possible to express the trip generation rate of each type as a function of the length of the line and the combined length of the lines that have a direct connection with it.

To do this, let $V_k$ be the number of boarding validations for line $k$ in some specific month, $l_k$ be the line’s length, and $l_{1,k}$ the combined length of the lines that connect with it at the time of observation (see Fig. A1). With the assumptions above, the number of validations should increase linearly with both $l_k$ and $l_{1,k}$. Thus, the proposed regression model is:

$$V_k = b_0 l_k^2 + b_1 l_k l_{1,k}$$ \hfill (A.1)

The model specification does not include a constant term because it would make little physical sense. If a lines’ length is zero, one should not expect any monthly validations. The first term of (A.1) represents the number of trips generated with destinations along the line, and therefore no transfers. This is the direct demand. The second term represents the number of boardings with origin (or destination) on line $k$ and destination (or origin) on the connecting lines. Note that only one half of these validations are outbound trips from line $k$. Thus, the formulas for total transfers, $X_k$, and total demand, $D_k$, generated by line $k$ are:

$$X_k = 1/2 b_1 l_k l_{1,k}$$ \hfill (A.2a)

$$D_k = b_0 l_k^2 + 1/2 b_1 l_k l_{1,k}$$ \hfill (A.2b)

So far we have assumed that we have a grid with a well-defined routing for each O-D pair. However, Barcelona is not a perfect grid, and there are a few locations where two lines overlap. This requires a modification of (A.1) because in the region of overlap some people can choose either of the two lines, and this provides a routing option that splits the demand. The modification should consider the length of overlap and take into account the overlapping lines’ frequency ratio in order to reflect such demand split.

On account of the overlap, the new model introduces two additional definitions of line lengths: the length of the overlap region, $l_{o,k}$; and the combined length of all lines that connect with this region, $l_{1,o,k}$. These two concepts are illustrated in Fig. A2, where the dashed line is the line that causes the overlap: $l_{o,k}$ is marked on the leftmost diagram; and $l_{1,o,k}$ on the rightmost (the case in the figure includes only one connecting line). It is also necessary to introduce $\eta_{o,k}$ as the fraction of buses flowing on the overlapping region that are not on line $k$; i.e., the ratio of the overlapping line frequency and the total frequency. This ratio is an approximation for the fraction of the demand that is syphoned away by the overlapping line. In
terms of headways, with $H_k$ representing the headway of line $k$ and $H_{o,k}$ the headway of the overlapping line, the expression is:

$$g_{o,k} = \frac{1}{H_{o,k}} - \frac{1}{H_k + 1/H_{o,k}}$$ (A.3)

With this notation, the specification for the demand of a line $k$ that experiences an overlap of length $l_{o,k}$ is:

$$V_k = \beta_{0,k}(l_k^2 - l_{o,k}^2\eta_{o,k}) + \beta_{1,k}(l_{1,k} - l_{o,k}l_{1,o,k}\eta_{o,k})$$ (A.4)

$$X_k = 1/2\beta_{1,k}(l_{1,k} - l_{o,k}l_{1,o,k}\eta_{o,k})$$ (A.5a)

$$D_k = \beta_{0,k}(l_k^2 - l_{o,k}^2\eta_{o,k}) + 1/2\beta_{1,k}(l_{1,k} - l_{o,k}l_{1,o,k}\eta_{o,k})$$ (A.5b)

The least squares regression method was then used to fit Eq. (A.4) to the data from each line and in this way obtain four sets of $\beta$-estimates. Table A1 summarizes these data for lines H6, V7 and V21. These lines do not exhibit significant overlaps and therefore, $l_{o,k} \equiv 0$. The table also includes the dependent variables $V_k$. Table A2 summarizes the data for line H12, which overlaps significantly with line H16. Therefore, the table includes its $l_{o,k}$, $l_{1,o,k}$ and $\eta_{o,k}$ values on separate rows.

A.2. Results

The following tables summarize the results obtained for each line (see Tables A3–A6).

Note from the tables that in all four cases the estimated parameters were statistically significant and the fit was good. Therefore, the parameter values were entered in (A.5) to predict the monthly number of passenger trips (and passenger trips with transfers) generated by each line in the four phases of the project, using the explanatory variables in Tables A1 and A2. Tables 2 and 3 of Section 4 in the text contain the results.

A.3. Discussion

All four models have similar explanatory power. The absolute value of the regression coefficients $\beta_{0,k}$ and $\beta_{1,k}$ differs between lines, and these differences are what one might expect. First, differences are expected since the demand levels for bus service are likely to be inhomogeneous throughout the city. Second, differences may be exacerbated because the impact of alternative transit modes may vary considerable across lines. For example, in the case of the Nova Xarxa, line
H12 lays precisely on top of alternative metro lines. This is probably why its $\beta_{0,k}$ coefficient is 41% smaller than that of line H6.

It is also interesting to see that the ratio $\beta_{1,k}/\beta_{0,k}$ differs considerably across routes. While it was approximately 0.08 for lines H6 and V21, it was about 0.20 for lines V7 and H12. This illustrates that the capacity of each line to generate direct and transfer trips varies considerably. In all cases, however, the direct demand predominates. Most of the variation is due to the $\beta_{0,k}$ coefficients, which change more drastically across lines. This seems reasonable since 0-transfer demand should depend on the line's location within the city, whereas transfer trips have a much broader area of influence, and should predominantly depend on the city's proclivity to transferring.

### References


### Tables

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<th>Table A3</th>
<th>Results for line H6.</th>
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<td>Regression model H6</td>
<td>R²</td>
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<td>Explanatory variable coefficient</td>
<td>Std. error</td>
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Transports de Barcelona, 2016. Private Communication.
